Enterococcus faecium Growth Model

Pavel ČERMÁK¹, Aleš LANDFELD², Pavel MĚŘÍČKA³ and Milan HOUŠKA²

¹General Teaching Hospital, Charles University, Prague, Czech Republic; ²Food Research Institute Prague, Prague, Czech Republic; ³Tissue Bank, Hradec Kralove Teaching Hospital, Hradec Kralové, Czech Republic

Abstract


Enterococci are bacteria commonly found in humans. However, these bacteria can cause severe infections in susceptible individuals. The strains of Enterococcus faecium have demonstrated an increasing resistance to antibiotics, which is considered an important virulence factor. The contribution of E. faecium to the infection-related illnesses has recently increased, which involves most of the isolated Vancomycin-Resistant Enterococcus (VRE) strains. Enterococci are common contaminants of human milk processed in milk banks, and the consumption of contaminated milk can cause severe infection-related complications if the control mechanisms fail to detect the contamination. Extensive data are available on the growth curves of E. faecium in broth at pH values between 6 and 7, at temperatures of 5°C to 20°C, and for water activity values \( a_w \) of 0.97 to 0.997. These growth curves were replaced with non-linear Gompertz curves for microorganism growth, the parameters of which were correlated with the temperature and pH values. A mathematical relationship to water activity could not be established since only two water activity levels have been experimentally tested and the resulting model would be highly inaccurate. The issue of water activity was resolved by the development of two separate models, one for each of the water activity values. The models correspond very well with the experimental growth curve data from which they were developed. The model for the water activity level of 0.997 was used to predict the growth of E. faecium in cow and human milks (these two fluids have practically identical water activity), and the prediction was compared to the experimental data. A good agreement between the predicted and experimental data was achieved for cow milk. With human milk, the model usually predicted a more rapid growth rate than that seen experimentally. The model was thus on the conservative side in all cases. The inhibitory agents naturally present in human milk might be responsible for the slower growth rates.

Keywords: Enterococcus faecium; microbial growth model; verification

In 1984, the Enterococcus family was described as a separate taxonomic unit and distinguished from streptococci; the distinction was based on DNA hybridisation data (Schleifer & Kilpper-Balz 1984). Today, the Enterococcus family includes 28 species (Klein 2003; Moreno et al. 2006). Microscopically, the organism is a Gram-positive, oval to slightly extended coccus that exists in pairs or short chains. It belongs to the facultative anaerobic organisms and does not develop spores or any visible capsule. Enterococci share a common polysaccharide antigen (\( \beta \)-glycerol-teichoic acid) which is bound to the cell wall. The cultivation of the microorganism is simple: the organisms

Supported by the Ministry of Agriculture of the Czech Republic, Projects No. 1B44040 and No. MZE 0002702201.
can grow on basic substrates used in microbiological laboratories at 10–45°C, with the optimum temperature of about 37°C. The microorganism can tolerate increased concentrations of NaCl (up to 6.5%) and bile salts (up to 40%), as well as higher substrate pH values (up to pH 9.6). The microorganism can withstand heating to 60°C for 30 minutes. Most enterococci proliferate under common aerobic conditions. Several species are supported in growth by 10% CO₂ in the incubation environment (MOTLOVÁ 1997).

Enterococci are part of the intestinal flora of numerous animal species. They have been used as probiotic agents to inhibit pathogenic microorganisms in the intestine, to stimulate the immune system, and to reduce blood cholesterol levels. E. faecium SF68 has been used as an alternative to antibiotic therapy to treat diarrhoea (LEWENSTEIN et al. 1979). However, long-term effects of enterococci on reducing the contents of low-density lipoproteins, (LDL)-cholesterol, have not been demonstrated (AGERHOLM–LARSEN et al. 2000).

The pathogenicity of enterococci is relatively low under normal conditions. Enterococci are considered dangerous agents because of their extreme resistance to the negative external influences and resistance to antibiotics (VOTAVA 2003). They are considered conditionally pathogenic and are important in nosocomial infections and super-infections, such as endocarditis, bacteremia, urinary tract infections, central nervous system infections, intra-abdominal abscesses, and infections in newborn infants (BENEŠ 1997; KLEIN 2003). Enterococci are a common cause of bacteremias (ČERMÁK et al. 2004). The urogenital tract, bile duct, and abdominal cavity are the most likely sites of infections. Endocarditis develops in approximately one-third of enterococcal bacteremia patients (KLEIN 2003). Enterococci cause approximately 12% of nosocomial infections (LINDEN & MILLER 1999). These infections develop in two stages. The initial stage usually involves asymptomatic colonisation of the skin and the gastrointestinal tract with an endemic strain contracted in a hospital environment. If the patient is receiving immunosuppression therapy, the size of the enterococci population may increase when the microorganisms proliferate from the initial colonisation sites, and thereby trigger a complicated infection (KAYSER 2003).

The pathogenicity of enterococci is relatively low under normal conditions. Enterococci are considered dangerous agents because of their extreme resistance to the negative external influences and resistance to antibiotics (VOTAVA 2003). They are considered conditionally pathogenic and are important in nosocomial infections and super-infections, such as endocarditis, bacteremia, urinary tract infections, central nervous system infections, intra-abdominal abscesses, and infections in newborn infants (BENEŠ 1997; KLEIN 2003). Enterococci are a common cause of bacteremias (ČERMÁK et al. 2004). The urogenital tract, bile duct, and abdominal cavity are the most likely sites of infections. Endocarditis develops in approximately one-third of enterococcal bacteremia patients (KLEIN 2003). Enterococci cause approximately 12% of nosocomial infections (LINDEN & MILLER 1999). These infections develop in two stages. The initial stage usually involves asymptomatic colonisation of the skin and the gastrointestinal tract with an endemic strain contracted in a hospital environment. If the patient is receiving immunosuppression therapy, the size of the enterococci population may increase when the microorganisms proliferate from the initial colonisation sites, and thereby trigger a complicated infection (KAYSER 2003).

The most common causative agents of enterococcal infections in humans are E. faecalis (80–90%) and E. faecium (5–10%). Infections with other species of enterococci are rather rare (KLEIN 2003). Enterococci do not have a single virulence factor, such as is the toxin in cholera, instead they have several virulent factors including enzymes (gelatinase, hyaluronidase), colonisation factors (adhesines (adhesins), surface proteins (Enterococcal surface protein – Esp), aggregation substance (AS), and cytolysine (cytolysin). Some strains of E. faecalis and E. faecium can produce extracellular super oxide, which facilitates the penetration of the bacteria into tissues and into the bloodstream (HYUCKE 1995). Enterococci can also rapidly acquire the resistance to antibiotics, and this is considered to be one of the key factors in their virulence (FRANZ et al. 2003; KAYSER 2003). In the USA, as many as 80% of all E. faecium strains have become resistant to penicillin-related antibiotics (HYUCKE et al. 1998), and this figure is 76% in Europe (KRESKEN et al. 2000). In recent years, the bacteria have developed resistance to previously effective antibiotics – aminoglycosides, cephalosporins, chloramphenicol, erythromycin, tetracycline, fluorochinolone, and glycopeptides (KLEIN 2003). Vancomycin-resistant enterococci (VRE) present a serious risk and a difficult problem, since they are resistant to all standard preparations used for the treatment of enterococcal infections. The resistance to vancomycin is related to the vanA, vanB, and vanC genes. The genes vanA and vanB are transferred via plasmids and cause an increased resistance among enterococci (MURRAY 1997, 1998) as well as other pathogens such as Staphylococcus aureus (WEIGEL et al. 2003). One of the sources of VRE is the use of growth-stimulating agents in the livestock production (AARESTRUP 1999). Another cause of the increasing numbers of VRE is the excessive use of antibiotics (HEATH et al. 1996; KOLAR et al. 2006a).

In the past, the main bacterial cause of human enterococcal infections was E. faecalis (in more than 80% cases), with E. faecium causing the remaining infections (JETT et al. 1994).

E. faecium has traditionally been considered to present fewer risks and a lower occurrence of the virulence factors as compared with E. faecalis (FRANZ et al. 2003). In recent years, a change in the trend has been recorded and the strains of E. faecium, in particular VRE strains, have become the main causes of enterococcal bacteremia (MUNDY et al. 2000). In the Czech Republic, the strains of E. faecium are predominant among VRE enterococci isolated from hospital in-patients.
Enterococci are often isolated from human milk processed in milk banks since their high levels of resistance allow the microorganisms to survive the procedures used to process human milk. The consumption of contaminated human milk can cause serious infections since it is usually intended for patients that are already susceptible to infections. Complications caused by the infection in a newborn, resulting from a resistant strain of \textit{E. faecium}, may present a particularly difficult treatment issue, especially in the cases of life-threatening infections. Therefore, the knowledge of the various characteristics of \textit{E. faecium} is of immense significance since it would allow for improved processing, storage, and transport of human milk.

It is particularly important to understand the risks of proliferation of small numbers of \textit{E. faecium} surviving careful pasteurisation. Related to this, it is also important to understand the thermal inactivation characteristics of \textit{E. faecium}. These characteristics were the subject of a previous study (Špelina et al. 2007).

The aim of this work is to provide an overview of the growth curves and a mathematical growth model for \textit{E. faecium} CCM 2308. The growth-related parameters were altered as follows: temperature 5–20°C, pH 6–7, and water activity at 0.97 and 0.997. The growth data were processed mathematically to obtain the parameters for a suitable mathematical growth model for the microorganism. These parameters were subsequently correlated as a function of temperature, pH, and water activity. The resulting mathematical model was tested against the growth data acquired for the same microorganism experimentally, using cow and human milk samples.

MATERIAL AND METHODS

\textbf{Broth inoculation}. A strain of \textit{E. faecium} CCM 2308 was selected from a collection of microorganisms. The culture of \textit{E. faecium} CCM 2308 was supplied by the Czech Collection of Microorganisms (CCM) in the form of gel plates contained in sterile vials. From each plate, a revitalised culture was prepared on an agar slant using the procedure recommended by the CCM.

The revitalisation of the culture proceeded at 37°C for 20 hours. Two colonies were taken from the revitalised culture and suspended in 1.8 ml saline. After a thorough mixing of the bacterial suspension, 0.2 ml was extracted and transferred to 1.8 ml of sterile saline in a test tube. After shaking, 1 ml was withdrawn from the solution and placed in a bottle with 500 ml of the nutrient substrate. After thoroughly shaking the nutrient broth, 0.1 ml of the broth was inoculated onto a Petri dish with blood agar. The number of colonies grown on the agar was taken as the initial concentration. The nutrient broth was cultivated at 5, 10, 15, and 20°C in a special thermal box, which enabled a highly accurate temperature control. The device was equipped with a fan ensuring a steady air circulation, and with an internal thermometer for the temperature monitoring and control at a specified position in the box.

The cultures were grown at the specified temperature for varying lengths of time. All cultures were grown independently and simultaneously in three bottles, producing three growth curves for each set of conditions (temperature, initial pH of the sterilised broth, and water activity).

\textbf{Samples collection and microorganism number determination}. The samples used to determine the microorganism numbers were collected aseptically, in time series, at 5°C, only after more than 1000 hours. When collecting the samples, the pH of the collected sample was also determined.

\textbf{Sample dilution}. After a thorough shaking of the bacterial suspension (cultivated broth), 0.2 ml was taken from the suspension and transferred to 1.8 ml of sterile saline in a test tube. Up to nine dilutions were obtained in this manner as necessary. Each of the dilutions was inoculated onto three Columbia blood agar plates.

\textbf{Inoculation and incubation of blood agar}. A 0.1 ml sample of each dilution was spread on an agar plate and inoculated using a plastic loop. The dishes were clearly marked and incubated in a thermostatic box for 24 h at 37°C. The numbers of colonies for each dilution were counted after incubation. Two plates were used for each dilution.

\textbf{Calculation method}. For the calculation purposes, plates and dilutions were selected to meet the conditions outlined below. In calculating the numbers of viable \textit{E. faecium}, the recent wording of the standard CSN ISO 7218:1998 was applied, which includes the amendment Amd.1:2001 and specifies a general formula for the calculation of a weighed average as follows:
\[ N = \frac{\Sigma C}{V \times [n_1 + (0.1 \times n_2)] \times d} \]

where:
- \( \Sigma C \) – sum of the colonies from all plates selected for the calculation from two successive dilutions, while at least one of the plates must contain at least 15 colonies
- \( V \) – volume (ml) of the inoculum transferred to each plate
- \( n_1 \) – number of plates selected for the calculation from the first dilution selected
- \( n_2 \) – number of plates selected for the calculation from the second dilution selected
- \( d \) – dilution factor corresponding to the first dilution selected for the calculation

If the condition for \( \Sigma C \) (i.e. at least one plate must contain at least 15 colonies) was not met, the value obtained was interpreted in line with the above-cited ISO standard – as an estimate.

**RESULTS AND DISCUSSION**

**Growth model**

The data selected for the growth curves are shown in Figures 1–4 to illustrate the curve shapes. The growth data were acquired for water activities of 0.97 and 0.997, and temperatures of 5, 10, 15, and 20°C. pH values shifted during the cultivation from the initial value, and increased by approximately 0.3 from the value measured after sterilisation of the broth. It was therefore decided to determine an average pH value for the whole cultivation process. These average values are listed in the relevant legend for each figure and in Table 1. Each cultivation was repeated three times, see figures. At 20°C, pH ~ 5.99, and water activity of 0.97, there was no measurable growth of micro-organisms due to a significant undetectable error. These data were not included in the development of the mathematical model.

All data obtained for the same initial pH, water activity, and temperature conditions were evaluated together. Datafit software (Oakdale Engineering, Oakdale, USA) was used to obtain the parameters of the growth curves using non-linear regression analysis.

Microbial growth modelling uses the Gompertz model, the modified Gompertz model, or the logistic curve (Zanoni et al. 1993). The Gompertz model was preferred in this case, provided that parameter \( a \) was considered a regression parameter. The following model was used:

\[
\log N = a + c \times \exp (- \exp(- b \times (t - m)))
\]

where:
- \( a \) – model parameter approximating the log of the initial concentration
- \( c \) – logarithm of the microorganism growth from the initial concentration to the stationary growth stage
- \( b \) – relative microorganism growth rate during the logarithmic growth stage
- \( m \) – time to maximum growth rate
- \( t \) – time (h)

![Figure 1. Growth curve for broth with \( a_w = 0.97, \) pH = 6.58, \( T = 5^\circ C \)]
The duration of the lag stage (the time when the organism adapts to the environment and does not proliferate) was calculated by: lag stage = \( m - \left(\frac{1}{b}\right) \).

By substituting this time for time \( t \) in the formula (3–1), it can be shown that at the end of the lag stage, the model predicts a slight increase in the numbers of microorganisms, i.e. by 0.067 of the value of \( c \).

\[
\log N = a + c \times e^{-e} = a + c \times 0.067
\]

Technical reasons prevented obtaining the same initial concentration of the microorganism, thus it was necessary to convert the regression parameters to a specified initial concentration to facilitate the correlation with temperature, pH, and water activity.

The specified initial concentration was \( a_2 = \log N_0 = 1 \) (\( N_0 = 10 \)). The formula for the calculation of parameter \( a \) involves determining \( t = 0 \) in formula (3–1):

\[
a = \log N_0 - c \times \exp (-\exp(b \times m))
\]

The conversion also ensures that the growth model converges to the same maximum microorganism concentration.

For the conversion, the relationships determined from the comparisons of the growth curves were used, describing two growth curves starting from the conditions marked with indexes 1 and 2. It was assumed that the parameters of the growth curve model indexed 1 are known, as they were specified by data regression for the initial concentration \( a_1 \). The second initial concentration \( a_2 \) was selected arbitrarily. Model 1 and model 2 must demonstrate the same duration for the lag stage. It therefore follows that:

\[
m_1 - \left(\frac{1}{b_1}\right) = m_2 - \left(\frac{1}{b_2}\right)
\]

from which \( m_2 \) can be easily determined

\[
m_2 = m_1 - \left(\frac{1}{b_1}\right) + \left(\frac{1}{b_2}\right)
\]

If there are equal maximum concentrations of microorganisms:

<table>
<thead>
<tr>
<th>Temperature (°C)</th>
<th>pH (–)</th>
<th>( a_1 ) (log CFU/g)</th>
<th>( b_1 ) (h(^{-1}))</th>
<th>( c_1 ) (–)</th>
<th>( m_1 ) (h)</th>
<th>Lag stage (h)</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>5.95</td>
<td>0.970</td>
<td>2.632</td>
<td>0.003861</td>
<td>7.126</td>
<td>419.1</td>
</tr>
<tr>
<td></td>
<td>6.26</td>
<td>0.970</td>
<td>2.307</td>
<td>0.004614</td>
<td>7.125</td>
<td>344.8</td>
</tr>
<tr>
<td></td>
<td>6.58</td>
<td>0.970</td>
<td>2.927</td>
<td>0.004841</td>
<td>7.415</td>
<td>335.7</td>
</tr>
<tr>
<td></td>
<td>5.86</td>
<td>0.997</td>
<td>2.414</td>
<td>0.003791</td>
<td>7.571</td>
<td>372.9</td>
</tr>
<tr>
<td></td>
<td>6.22</td>
<td>0.997</td>
<td>1.843</td>
<td>0.003919</td>
<td>7.922</td>
<td>343.4</td>
</tr>
<tr>
<td></td>
<td>6.60</td>
<td>0.997</td>
<td>1.925</td>
<td>0.003671</td>
<td>7.792</td>
<td>274.3</td>
</tr>
<tr>
<td></td>
<td>5.93</td>
<td>0.970</td>
<td>2.592</td>
<td>0.010884</td>
<td>7.449</td>
<td>153.5</td>
</tr>
<tr>
<td></td>
<td>6.35</td>
<td>0.970</td>
<td>2.899</td>
<td>0.013603</td>
<td>7.142</td>
<td>119.4</td>
</tr>
<tr>
<td></td>
<td>6.56</td>
<td>0.970</td>
<td>2.706</td>
<td>0.012059</td>
<td>7.254</td>
<td>130.0</td>
</tr>
<tr>
<td></td>
<td>5.93</td>
<td>0.997</td>
<td>2.582</td>
<td>0.015595</td>
<td>7.690</td>
<td>99.6</td>
</tr>
<tr>
<td></td>
<td>6.30</td>
<td>0.997</td>
<td>2.920</td>
<td>0.017175</td>
<td>7.534</td>
<td>90.4</td>
</tr>
<tr>
<td></td>
<td>6.55</td>
<td>0.997</td>
<td>2.756</td>
<td>0.016824</td>
<td>7.621</td>
<td>94.2</td>
</tr>
<tr>
<td></td>
<td>5.99</td>
<td>0.970</td>
<td>3.154</td>
<td>0.031482</td>
<td>6.999</td>
<td>56.7</td>
</tr>
<tr>
<td></td>
<td>6.28</td>
<td>0.970</td>
<td>3.292</td>
<td>0.028514</td>
<td>7.158</td>
<td>53.4</td>
</tr>
<tr>
<td></td>
<td>6.56</td>
<td>0.970</td>
<td>3.434</td>
<td>0.028105</td>
<td>7.153</td>
<td>55.8</td>
</tr>
<tr>
<td></td>
<td>5.94</td>
<td>0.997</td>
<td>3.131</td>
<td>0.055135</td>
<td>7.490</td>
<td>26.1</td>
</tr>
<tr>
<td></td>
<td>6.22</td>
<td>0.997</td>
<td>2.770</td>
<td>0.059784</td>
<td>7.480</td>
<td>25.0</td>
</tr>
<tr>
<td></td>
<td>6.55</td>
<td>0.997</td>
<td>2.917</td>
<td>0.056246</td>
<td>7.472</td>
<td>27.5</td>
</tr>
<tr>
<td></td>
<td>6.4</td>
<td>0.997</td>
<td>2.948</td>
<td>0.101110</td>
<td>7.349</td>
<td>16.2</td>
</tr>
<tr>
<td></td>
<td>6.67</td>
<td>0.997</td>
<td>2.964</td>
<td>0.088648</td>
<td>7.431</td>
<td>15.5</td>
</tr>
<tr>
<td></td>
<td>6.99</td>
<td>0.997</td>
<td>3.267</td>
<td>0.098031</td>
<td>7.423</td>
<td>16.2</td>
</tr>
</tbody>
</table>
\[ a_1 + c_1 = a_2 + c_2 \]

Hence, the value of parameter \( c_2 \) is:
\[ c_2 = a_1 + c_1 - a_2 \quad (3-3) \]

The maximum growth rate \( \frac{d \log N}{dt} \) is achieved at time \( t = m \). This can be proven with the second derivation of equation (3–1) and setting the condition \( d^2 \log N/dt^2 = 0 \). The maximum growth rate is then determined by the formula:

\[ \frac{d \log N}{dt} = c \times b \times e^{-1} \quad (3–4) \]

If it is assumed that the model determines the same maximum growth rate for the logarithmic stage (regardless of the initial microorganism concentration), formula (3–4) leads to:

\[ c_1 \times b_1 = c_2 \times b_2 \]

Hence, the new value of \( b \) can be obtained by:
\[ b_2 = b_1 \times c_1 / c_2 \quad (3–5) \]

The resulting values of the converted model parameters are shown in Table 1. The data indicate the effects of temperature, pH, and water activity on the model parameters. Table 1 also shows that the data for 2°C and water activity 0.97 were discounted, since this particular experiment was affected by a serious error.

The values obtained for parameters \( b, c \) and \( m \) were correlated with temperature, pH, and water activity using multiple non-linear regression analysis (Datafit software). It was found that the correlations with the water activity were highly unreliable. For this reason, it was decided to develop two separate mathematical models, one...
for each of the water activity values. The model parameters are therefore valid for specific water activity values. Table 1 shows that the values of parameter \(c\) remain almost constant. The correlation of parameter \(c\) with temperature and pH will therefore be rather unreliable. For the purposes of higher prediction accuracy, it was nonetheless decided to correlate this parameter as a function of temperature and pH.

The following relationships and values were obtained for the constants of regression dependencies. Letters \(a–f\) are used to represent the empirical constants of the dependences on pH and temperature (parameters of secondary models). To differentiate between the parameters of the Gompertz model and the empirical constants of temperature and pH dependences, the Gompertz model parameters are marked in bold.

For water activity in nutrient broth \(a_w = 0.97\), the following relationships and constants were obtained \((R^2 = 0.99)\):

\[
\begin{align*}
\mathbf{b} &= a + b \times T + c/pH + d \times T^2 + e/pH^2 + f \times T/pH \quad (3–6) \\
\end{align*}
\]

where:
- \(T\) – temperature (°C)
- \(a = -0.215; b = -5.700 \times 10^{-3}; c = 3.026; d = 1.870 \times 10^{-4}; e = -10.253; f = 2.790 \times 10^{-2}\)

For parameter \(c\), the following formula applies \((R^2 = 0.16)\):

\[
\begin{align*}
\mathbf{c} &= a + b \times T + c \times pH \\
\end{align*}
\]

\(a = 6.636; b = 1.20 \times 10^{-2}; c = 0.109\)

For parameter \(m\), the following formula applies \((R^2 = 0.99)\):

\[
\begin{align*}
\mathbf{m} &= a \times T^b \times pH^c \\
\end{align*}
\]

\(a = 258.963.6; b = -1.553; c = -2.215\)

For water activity in the nutrient broth \(a_w = 0.997\), the following relations and empirical constants apply \((R^2 = 0.99)\):

\[
\begin{align*}
\mathbf{b} &= a + b \times T + c \times T^2 + d \times T^3 + e \times pH \\
\end{align*}
\]

\(a = 4.880 \times 10^{-2}; b = -1.660 \times 10^{-2}; c = 1.730 \times 10^{-3}; d = -3.920 \times 10^{-5}; e = -9.580 \times 10^{-5}\)

For parameter \(c\), the following formula applies \((R^2 = 0.76)\):

\[
\begin{align*}
\mathbf{c} &= a + b \times T + c \times pH \\
\end{align*}
\]

\(a = 7.304; b = -2.690 \times 10^{-2}; c = 9.390 \times 10^{-2}\)

For parameter \(m\), the following formula applies \((R^2 = 0.99)\):

\[
\begin{align*}
\mathbf{m} &= a \times T^b \times pH^c \\
\end{align*}
\]

\(a = 562.055.8; b = -1.958; c = -2.348\)

The values obtained for parameter \(b\) as a function of temperature \(T\) and pH for different water activity values are not of the same type. Formula \((3–6)\) includes a complicated dependency on pH and temperature, whereas for water activity 0.997 it is more suitable a rather simple formula \((3–9)\), which contains a parabolic third degree dependency on temperature and linear dependency on pH.

Parameter \(c\) has a linear dependence on temperature as well as on pH. For water activity 0.97, the...
The correlation coefficient is not significant because the critical value of the correlation coefficient for the number of the degrees of freedom $9 - 3 = 6$ at the significance level of 95% is 0.707. For water activity 0.997, there are 12 data points, the number of model parameters is also 3, and the number of the degrees of freedom is therefore 9. The critical value of the correlation coefficient at 95% significance level is 0.602, and the correlation obtained (formula 3–10) is therefore statistically significant (Štěpánek 1975).

Parameter $m$ is expressed by a power expansion that is dependent on both temperature and pH. The correlations for the water activity values examined have significant correlation coefficients.

Figures 1–4 show the Gompertz curves representing the regression curves obtained from the data shown. The figures also contain curves that represent a growth model that includes the effects of temperature and pH for the given water activity value. The figures show that the growth model is in a good agreement with the experimental data. The calculations of the growth model were based on the values of the initial concentrations $a_1$ as shown in Table 1. The values of other parameters determined by formulas (3–6) to (3–11) were also converted to the relevant initial average concentration $a_1$ for the calculation of particular growth curves.

**Model Verification**

Verification data for cow and human milks were measured also by our team (Figures 5–9). The data
were obtained for the same strain of *E. faecium*, i.e. CCM 2308.

The growth model for water activity 0.997 was used for all values of pH and temperature, and the theoretical growth curve of *E. faecium* was calculated. Figure 5 shows a model that is valid for cow milk at 5°C, and reveals a very good agreement between the experimental data and the model.

The same applies for cow milk at temperatures of 10°C and 20°C. Figure 6, which also includes the data for 15°C, shows that the model predicts a more rapid growth of microorganisms and a shorter duration of the lag phase than were those measured experimentally. Overall, it can be stated that the prediction of *E. faecium* growth in cow milk agrees well with the experimental data.

Figures 7–9 indicate that the predictions of microorganism growth and the experimental data obtained for human milk are in agreement. Figure 7 shows a model applicable for 5°C and shows a very good agreement between the model prediction and the experimental data. Figure 8 is valid for 10°C and shows that the model predicts a more rapid growth rate than was that measured experimentally. The experimental data also show a longer lag phase.

Figure 9 is valid for human milk at 20°C and shows a shorter lag phase for the model (growth rates approximately equal, plus a good agreement between both maximum concentrations). It should be noted that the experimental data used in this figure for milk sample 3 shows an extremely long lag time. This might be due to the inhibitory agents that are naturally present in human milk. In general, the model predicts for human milk more rapid growth rates in comparison to the experimental results, and therefore can be considered to be a conservative model.

**CONCLUSIONS**

Extensive data were obtained for *E. faecium* growth curves at pH values between 6 and 7, temperatures between 5–20°C, and water activities *a*_*w* of 0.97 and 0.997. These data were replaced with a non-linear Gompertz model for microorganism growth, whose parameters were correlated with temperature and pH. It was proved to be impossible to determine mathematical dependence on water activity since only two values were specified and the resulting model would be highly inaccurate. Therefore, two models were developed, one for each of the specified water activity values. These models show a good agreement with the experimental data for the growth curves.

The model for water activity 0.997 was used to predict *E. faecium* growth rates in cow and human milks (which have nearly the same water activities) and the predicted values were compared with the experimental data. There was a good agreement between the predicted and the experimental data for cow milk. As to human milk, the growth model tended to predict faster growth rates than were those measured experimentally. The model can therefore be considered conservative and erroneous on the side of caution and safety. The slower actual growth rates are likely due to the presence of natural growth inhibitors in human milk.
References


Štěpánek V. (1975): Matematická statistika v chemii. Praha, SNTL.


Received for publication April 18, 2008
Accepted after corrections May 18, 2009

Corresponding author:
Ing. MILAN HOUŠKA, CSc., Výzkumný ústav potravinářský Praha, v.v.i., Radiová 7, 102 31 Praha 10-Hostivař, Česká republika
tel.: + 420 296 792 306, fax: + 420 272 701 983, e-mail: milan.houska@vupp.cz