Increased interest in commodities, known as ‘commodity financialization’, has generated a gradual integration of agricultural commodity markets over the last decades, also influencing a rapid and steady growth of financial investments in these markets. Hamadi et al. (2017) contended that the so-called financialization of agricultural commodities took effect between 2004 and 2005. Numerous authors, such as Matošková (2011), Irwin and Sanders (2012) and Hernandez et al. (2014) claimed that agricultural commodity financialization had risen levels of correlation and volatility spillover among these assets. Hernandez et al. (2014) asserted that agricultural markets are highly interrelated and there are both own- and cross-volatility spillovers and dependence among most of the agricultural markets. Baldi et al. (2016) analysed agricultural commodities from the investors’ point of view. They asserted that investing in agricultural commodities is generally attributed to low correlation and interdependence with traditional asset classes, such as stocks and bonds, which allows for portfolio diversification benefits. This happens due to the fact that agricultural commodities are driven by some particular fundamentals, e.g. weather conditions, supply constraints in the physical production, various geopolitical events, higher oil prices, increasing demand for biofuels, and speculation, which impose different price patterns and dynamics to agricultural commodities in respect to traditional assets.

In the process of the dynamic correlation investigation between various assets, most researchers observed this interconnection only via time dimension (Ceylan and Gozde 2012), neglecting the frequency domain features, which is an important aspect for investors who act at different time horizons. Conlon and Cotter (2012) explained that the sample reduction problem arises when researchers try to match the frequency of data with the different time horizons, thus the multiscale analysis in the economy has been little studied in general.
In addition, very little is known about the mutual interdependence across agricultural commodities, according to Trujillo-Barrera et al. (2012), and there is even less knowledge about their dynamic nexus at higher scales. In that regard, this study endeavours to contribute to the literature by investigating thoroughly the nature of the dynamic interconnectedness between each pair of the five selected cereal spot commodities – wheat, corn, soybean, rice and oats, emphasising both time and frequency characteristics of their mutual nexus. Being sufficiently aware of the nature of the interlink between the selected agricultural commodities could serve well for various investors who combine agricultural commodities in their n-asset portfolio and act at different time-horizons. In order to provide such results, a wavelet coherence (WTC) method was used, which addresses both time and frequency domains, circumventing at the same time the problem of sample size reduction. The idea to utilise this method was borrowed from recent studies such as Barunik and Vacha (2013), Živkov et al. (2018) and Živkov et al. (2019). Dewandaru et al. (2014) claimed that the WTC methodology is particularly useful when researchers work with non-stationary signals that contain numerous outliers. In addition, the phase difference method of Aguiar-Conraria and Soares (2011) was applied to further analyse the lead/lag relationship between each examined pair of selected cereals in order to capture their spillover interconnections at particular time scale. To the best of our knowledge, very few papers scrutinised the interdependence among agricultural commodities, and none of the existing papers did an in-depth analysis of correlation and spillover effects via different frequency scales that exist between major cereal markets.

LITERATURE REVIEW

Since agricultural commodity prices began to exhibit considerably erratic behaviour between 2007–2008, the evolution of these movements has attracted attention in the media and academia alike. These markets are becoming more integrated because of globalisation, according to Sanjuan-Lopez and Dawson (2017), and thus the information about prices in one market is immediately transmitted electronically to others. Gilbert (2010a) contended that the demand for grains and oilseeds as biofuel feedstocks had been cited frequently as the main cause of the price rise. However, he found that the index based investment in agricultural futures markets is seen as the major channel through which the macroeconomic and monetary factors generated the 2007–2008 food price rises. Gilbert (2010b) argued that the observed change in food prices might be explained by financial activity in futures markets and various proxies for speculation. Adammer et al. (2017) analysed the long and short-run connection between North American and European agricultural futures markets. They found that the US markets lead in terms of price transmissions and volatility spillovers, but US markets, also, predominantly react to deviations from the long-run equilibrium which indicates a rising impact of the European agricultural markets.

The manuscript of Grieb (2015) investigated volatility spillover effects between nine physical commodity futures contracts (corn, rough rice, soybeans, wheat, feeder cattle, lean hogs, live cattle, West Texas Intermediate (WTI) oil and Henry Hub natural gas). He revealed a strong pattern of price spillovers, while corn demonstrated to be the commodity that most broadly received and transmitted both price and volatility spillovers, followed by crude oil. The results of Lahiani et al. (2014) concur in a great extent with the findings of Grieb (2015). They examined the return and volatility spillovers among the four major agricultural commodities (wheat, sugar, cotton and corn). Results indicated that there is evidence of significant return and volatility transmission across considered commodities and that the conditional volatility of corn has an important explanatory power on the volatility of the other commodities. The paper of Musunuru (2014) analysed price volatility linkages between two important agricultural commodities: corn and wheat. He found evidence of bidirectional linkages between corn and wheat in terms of returns and volatility, while multivariate conditional Student’s t-distribution results show a unidirectional volatility transmission from corn to wheat.

WAVELET COHERENCE AND PHASE DIFFERENCE

The wavelet technique estimates the spectral characteristics of a time-series as a function of time, revealing how the different periodic components of a specific time-series evolve. According to Dajčman (2012), the continuous wavelet transform $W_s(u, s)$ is obtained by projecting a specific wavelet $\psi(\cdot)$ onto the examined time series $x(t)$ which belongs to the Hilbert space $L^2(\mathbb{R})$ by the following expression:

$$W_s(u, s) = \frac{1}{\sqrt{s}} \int_{-\infty}^{\infty} x(t) \overline{\psi\left(\frac{t-u}{s}\right)} dt$$

(1)
where $u$ represents the position of the wavelet in the time domain while $s$ portrays the position in the frequency domain for a discrete time series $x(t)$, $t = 1, 2, ..., N$. From Equation 1, information on time and frequency can be simultaneously obtained by mapping the original time series into a function of $u$ and $s$ in the wavelet transform.

According to Vacha and Barunik (2012), squared wavelet coherence measures the local linear correlation between two stationary time series at each scale, and it is equivalent to the squared correlation coefficient in linear regression. Torrence and Webster (1999) explained that WTC can be presented as a squared absolute value of the smoothed cross wavelet spectra normalised by the product of the smoothed individual wavelet power spectra of each selected time series. The cross wavelet transform of two time-series, $x(t)$ and $y(t)$, is defined as $W_{xy}(u,s) = W_x(u,s) \overline{W_y(u,s)}$, wherein $W_x$ and $W_y$ are the wavelet transforms of $x$ and $y$, respectively. The squared wavelet coherence coefficient is given as follows:

$$R^2(u,s) = \frac{|S(s^{-1}W_{xy}(u,s))|^2}{S(s^{-1}W_x(u,s))^2 S(s^{-1}W_y(u,s))^2}$$

where $S()$ stands for a smoothing operator and $s$ is a wavelet scale. The squared wavelet coherence coefficient ranges at $0 \leq R^2(u,s) \leq 1$, whereby the values near zero point to weak correlation, while the values near one indicate a strong correlation. WTC is estimated by applying the Monte Carlo simulation methods.

One well-known lack of the WTC methodology is that it is unable to determine whether the dependence between two time-series is positive or negative because the wavelet coherence is squared. Therefore, wavelet coherence phase differences that enable to see details on the delays in the oscillation (cycles) between two agricultural time-series under study were additionally considered. Following Torrence and Webster (1999) the wavelet coherence phase difference is defined as follows:

$$\phi_{xy}(u,s) = \tan^{-1}\left(\frac{I\left\{S(s^{-1}W_{xy}(u,s))\right\}}{R\left\{S(s^{-1}W_{xy}(u,s))\right\}}\right)$$

where $I$ and $R$ are the imaginary and real parts, respectively, of the smooth power spectrum. The phase difference between the two series ($x, y$) is indicated by vector arrows on the wavelet coherence plots. Vacha and Barunik (2012) contended that right (left) pointing arrows indicate that the time series are in-phase (anti-phase) or are positively (negatively) correlated.

If arrows point to the right and up, the second variable is lagging and if they point to the right and down, the second variable is leading. Reversely, if arrows point to the left and up, the second variable is leading and if arrows point to the left and down, the second variable is lagging.

In addition, according to the explanation of Aguiar-Conraria and Soares (2011), if $\phi_{xy} \in (0, \pi/2)$ then the series move in phase, with the time-series $y$ leading $x$. On the contrary, if $\phi_{xy} \in (-\pi/2, 0)$ then it is $x$ that is leading. An anti-phase situation (analogous to negative covariance) happens if there is a phase difference of $\pi$ (or $-\pi$), meaning $\phi_{xy} \in (-\pi/2, \pi) \cup (-\pi, \pi/2]$. If $\phi_{xy} \in (\pi/2, \pi)$ then $x$ is leading, and the time series $y$ is leading if $\phi_{xy} \in (-\pi, -\pi/2)$. The phase difference of zero indicates that the time series move together (analogous to positive covariance) at the specified frequency.

**DATASET AND PRELIMINARY FINDINGS**

For the research purposes, the spot closing prices of the five major agricultural commodities were considered – corn, wheat, soybeans, rice, and oats. All daily agricultural prices are transformed into ln-returns according to $r_{it} = 100 \times \ln(P_{it}/P_{it-1})$, where $r_{it}$ is the agricultural return and $P_{it}$ is the closing price of a particular agricultural commodity at time $t$. The sample covers the period from January 1, 2000 to February 28, 2018, and all data were obtained from the Datastream (2018). Utilizing the wavelet coherence methodology, dynamic nexus in seven frequency levels was investigated, allowing us to observe dynamic interconnection in seven different time horizons, which corresponds to: scale 1 (2–4 days), scale 2 (4–8 days), scale 3 (8–16 days), scale 4 (16–32 days), scale 5 (32–64 days), scale 6 (64–128 days) and scale 7 (128–256 days). First two scales observe the short-term dynamics, midterm is represented by the third, fourth and fifth scales, while the sixth and seventh scales correspond to the long-term dynamics.

Table 1 presents concise, descriptive statistics that account first four moments and the results of the Jarque–Bera test (JB) for ln-return series. Also, empirical movements of the agricultural commodities in level and ln-returns are shown in Figure 1. It can be noticed that all the agricultural commodities have relatively similar dynamic patterns, that is, their prices rose till the outbreak of the world financial crisis, then plummeted in 2008 and recovered from 2010, which lasted till 2013. These preliminary findings might indicate that the pairwise correlations are relatively
Table 1. Summary statistics of selected agricultural commodities

<table>
<thead>
<tr>
<th></th>
<th>Mean</th>
<th>Standard deviation</th>
<th>Skewness</th>
<th>Kurtosis</th>
<th>JB</th>
</tr>
</thead>
<tbody>
<tr>
<td>Corn</td>
<td>0.013</td>
<td>1.844</td>
<td>-0.620</td>
<td>15.691</td>
<td>29 234</td>
</tr>
<tr>
<td>Wheat</td>
<td>0.010</td>
<td>2.034</td>
<td>0.133</td>
<td>4.950</td>
<td>695</td>
</tr>
<tr>
<td>Soybean</td>
<td>0.016</td>
<td>1.713</td>
<td>-1.019</td>
<td>20.465</td>
<td>55 576</td>
</tr>
<tr>
<td>Rice</td>
<td>0.021</td>
<td>1.699</td>
<td>-0.551</td>
<td>17.278</td>
<td>36 823</td>
</tr>
<tr>
<td>Oats</td>
<td>0.016</td>
<td>2.458</td>
<td>-1.126</td>
<td>14.791</td>
<td>25 906</td>
</tr>
</tbody>
</table>

JB – value of Jarque-Bera coefficients of normality
Source: authors’ calculation

Figure 1. Empirical dynamics of selected agricultural commodities

X-axis stands for years, left Y-axis denotes percentage, while right Y-axis indicates the price of the agricultural commodities; grey line denotes log returns of the agricultural commodities, while black line explains the empirical dynamics of the agricultural prices
Source: authors’ calculation
high, which mitigates diversification possibilities in the agricultural markets. Table 1 reveals that the highest average returns are obtained in rice, while standard deviation values indicate that oats are the riskiest agricultural commodity. Left skewness and high kurtosis are dominant among selected assets, which justifies the usage of wavelets, since this methodology can tackle outliers, but also can remove noises in the original data (Dewandaru et al. 2014). The JB test confirms the non-normality characteristics of agricultural commodities.

### WAVELET COHERENCE RESULTS

This section presents the results of the pairwise wavelet coherence\(^1\) plots between the five selected agricultural commodities. The wavelet technique can assess the strength of the interdependence both in time and frequency domains. The horizontal axis denotes time component in our WTC plots, while the left vertical axis represents the frequency component, which goes up to the seventh scale (256 days). The strength of the co-movement between each of the selected agricultural commodities is gauged via colour surfaces, whereby blue and green colours signify low coherence, while warmer colours point to higher coherence. The colour pallet is presented at right Y-axis, and it ranges from 0 to 1. The cone of influence marks the area of statistical significance at the 5% level obtained from the Monte Carlo simulations.

Figure 2 reveals that cooler, that is, low correlation colours are dominant at high-frequency scales in all WTC plots. It implies that market-specific or idiosyncratic characteristics prevail in short-term. Although relatively unison movements of daily agricultural prices are found in Figure 1, the WTC plots do not show that a strong correlation exists between agricultural commodities at higher frequency scales, that is, shorter time-horizons. These results are in line with the findings of Sanjuan-Lopez and Dawson (2017), who contended that market microstructure models and the efficient markets hypothesis tend to have a major role in agricultural markets, whereby both private and public information becomes immediately compounded in prices because of electronic trading. Our results indicate that strong coherence islands are present between some agricultural commodities, but it appears evident only at higher wavelet scales, i.e. from 32 days onwards. For example, it is particularly apparent for the corn-wheat, corn-soybean, wheat-soybean, wheat-rice and rice-soybean cases. High coherence at lower frequency scales suggests that fundamentals rather than idiosyncratic factors most likely mould the dynamics and the interrelationship between the selected cereals. This stance is in line with the findings of Gilbert (2010a), who contended that common factors, relating to demand growth, monetary and financial developments, are likely to be the main determinants of changes at the overall level of agricultural prices. In addition, he claimed that oil price and the dollar exchange rate movements had been important causal factors as well, but the impact of the former has varied over time, whereas exchange rate effects are relatively small.

High coherence areas are visible at higher scales, but it should be said that, in some instances, high correlations are visible even at the low scales, up to 32 days. Most striking cases in which higher coherence is visible at higher frequencies are corn-wheat, corn-soybean, corn-oats and wheat-oats. These findings could lead to the assumption that monetary and financial activities could have some influence occasionally on grain prices over recent years. According to Figure 1, the boom in agricultural prices occurred in the 2006–2008 period, which took place in the context of enormous world liquidity, resulting from large US trade deficits and loose monetary policies. In the ‘post-Lehman’ months, the majority of the agricultural commodities prices saw sharp falls over the second half of 2008, which instigated high coherence as well. However, these results most likely do not reflect a direct causal link between agricultural assets, but rather common causation is a probable culprit. The increased interest in commodities, as a favourable asset class, before the world financial crisis was mostly stimulated by the general rise of energy, metal and agricultural prices. Agricultural investments are the activities that are sufficiently large to move prices and to induce negative shocks to the limited agricultural inventories, galvanizing the inflation of food commodity prices. By all odds, the strong agricultural comovement does not happen immediately, but it comes at some delayed period, that is, at higher wavelet scales. However, in some cases, high coherence areas can be found even at the higher frequencies, but these are isolated phenomena. High coherence at lower wavelet scales might be the aftermath of the financial activity in futures markets and various proxies for speculation.

---

\(^1\)Wavelet coherence is calculated via the ‘WaveletComp’ package in R.
Figure 2. Pairwise wavelet coherence plots between five agricultural commodities
left Y-axis denotes wavelet scales expressed in days, while right Y-axis explains the strength of the coherence via colour pallet
Source: authors' calculation
as explained by Cipra (2010) and Gilbert (2010b). Von Braun and Tadesse (2012) supported this stance, arguing that speculation effects could be stronger than demand- and supply-side shocks.

From the investors’ perspective, our WTC findings may indicate which agricultural commodities would serve well for diversification purposes in an n-asset portfolio. For investors who rebalance their portfolio in the short term (up to three weeks), all analysed cereals can be comprised in a portfolio, since all agricultural commodities have very low coherence between themselves at high frequencies. On the contrary, investors who take their positions at somewhat longer time-period must contemplate more carefully which agricultural commodities are convenient to combine in a portfolio and which ones should be avoided, due to the presence of strong coherence that exists between some cereals at higher wavelet scales. For instance, our WTC results suggest that long term investors should not combine in one portfolio following pairs – corn and wheat, corn and soybean, wheat and soybean, and rice and soybean. One combination that particularly stand out among others and which would be suitable for all investors, regardless of which time-horizon they pursue, is a corn-rice pair. This pair has the lowest level of high coherence areas at all wavelet scales according to the WTC plots, whereas rice-oats, oats-soybean and corn-oats follow.

PHASE DIFFERENCE RESULTS

WTC plots provide good insight regarding the strength of coherence, which is an important input for the effective diversification realization. Also, WTC plots bear some information regarding the lead/lag relationship between the analysed series, and it is stored in phase-arrows of the WTC plots. One shortcoming with phase-arrows is that they can be seen only in strong coherence areas, while in other, lower coherence regions, phase arrows shift direction constantly, without a common and stable behaviour. In such circumstances, researchers cannot precisely make out which variable is lagging or leading the other one at higher frequency scales. In addition, it should be said that a strong minimal phase difference does not exist under minimum dependency. So, in order to avoid the phase difference biases, phase difference was calculated only at longer terms, because WTC plots suggest a stronger presence of high coherence at longer time-horizons. This particular method carries the information regarding the direction of the coherence, discloses the average lead/lag relationship dynamics through the entire sample-period, and ultimately indicates from which agricultural market spillover shocks originate. Dajčman (2013) addressed this issue, explaining that this information is useful for international investors since if they know empirically that one time-series leads the other one, then its realisations may be used to forecast the realisations of the lagging time series. Figures 3–4 present phase difference plots between the selected agricultural commodities at the 64–128 and 128–256 days frequency bands.

Figures 3–4 depict pairwise phase difference dynamics at the frequency range of 64–128 and 128–256 days, and it is obvious that shapes of phase differences in Figures 3–4 are relatively stable and long-lasting. All these characteristics create a good foundation for the appraisal of the lead/lag relationship between selected cereals since this information could be of a paramount significance for investors in terms of investments in agricultural markets and portfolio selection. When it is clear which variable empirically leads the other one, then this information may be used to take an investment position in the lagging time series. With this type of knowledge, global investors can achieve higher returns in an n-asset portfolio.

Figure 3 describes the lead/lag nexus at the 64–128 days frequency band, and it can be seen that in some instances a stable and prolonged lead/lag patterns exist between some agricultural commodities. For example, the most unambiguous relation has corn and soybean. Phase differences of these cereals are continuously above zero since 2002, which undoubtedly suggests that developments in the soybean market precede the corn dynamics. Corn and wheat also have a relatively stable relationship since 2010, whereby corn is a commodity that has a leading role. In the case of corn and rice, rice leads corn since 2010. Striking dynamics can also be seen in the case of wheat and rice since 2003. In this case, phase difference has a very stable positive values from that year, which is clear indication that wheat is a lagging cereal. An interesting relationship have rice and oats, whereby it can be seen that phase difference frequently breaches $-\pi/2$ boundary, which is a sign that these two cereals found themselves quite often in an antiphase situation, and that is good for hedging purposes. In the cases of

---

2The results are obtained by applying the ASToolbox of Aguiar-Conraria and Soares (2011).
Figure 3. Phase difference plots of agricultural commodities at 64–128 days frequency band
left Y-axis denotes phase difference domain, which spreads from $\pi$ to $-\pi$
Source: authors’ calculation
Figure 4. Phase difference plots of agricultural commodities at 128–256 days frequency band

left Y-axis denotes phase difference domain, which spreads from $\pi$ to $-\pi$

Source: authors’ calculation
other agricultural pairs, no steady lead/lag relationships were found at the sixteenth wavelet scale (64–128 days frequency band).

Figure 4 presents the phase difference results at the longest time-horizon. These findings seem very similar to the results found in Figure 3, but some discrepancies have also been reported. For instance, soybean constantly leads corn dynamics in the longest time-horizon, which is consistent with the findings presented in Figure 3. On the other hand, in corn versus wheat plot, it is no longer so obvious which cereal has a dominant leading/lagging role, but it is more likely that both cereals follow the same homogeneous path, since the phase difference oscillates around zero from 2008. In the corn-rice and corn-oats plots, the results are pretty inconclusive, because lead/lag positions shift throughout the full-sample. It also applies for the wheat-soybean, wheat-rice, wheat-oats and rice-soybean pairs. At the 128–256 frequency band, rice and oats no longer report antiphase relations, which is different comparing to the findings in Figure 3. However, it is clear that rice has a dominant role till 2015, while from 2015 oats gains the upper hand. In the case of oats-soybean, it is apparent that phase difference is above zero since 2002, which suggests that soybean has a strong leading role from that year onwards.

CONCLUSION

This paper investigates the interdependence between the five spot agricultural commodities at different time-horizons. Two innovative and complementary methodologies were used – wavelet coherence and phase difference. The WTC results show the absence of strong coherence between agricultural commodities at higher frequency scales, but dark red islands were found between some agricultural commodities at longer time-horizons. High coherence at lower frequency scales suggests that common factors, that is, monetary and financial activities, are most likely the causes that have affected the comovements of the grain prices over the recent years. It is particularly apparent for the corn-wheat, corn-soybean, wheat-soybean, wheat-rice and rice-soybean cases.

The phase difference approach provides the information regarding lead/lag relationship dynamics throughout the entire sample-period, and it shows from which agricultural market spillover shocks have come from. This type of knowledge is particularly useful for agricultural asset selection in terms of gaining profit, because the information about the leading variable may be used to forecast the realisations of the lagging one. A stable pattern of the phase difference can be seen at longer time-horizons, i.e. at the 64–128 and 128–256 frequency bands, whereby corn-soybean, corn-wheat, corn-rice and rice-oats are the pairs in which a clear and stable lead/lag relationship is present. More specifically, corn is the commodity that frequently lags most of all other listed cereals, while oats is a commodity that leads rice for most of the time.

Combining the findings from the wavelet coherence and phase difference methods, it can be suggested which cereals are the most appropriate to be found in an n-asset portfolio. According to evidence, at the 128–256 frequency band, corn and oats constantly and very steadily lag soybean. Therefore, observing the movements of soybean, future dynamics of corn and oats can be predicted, and thus these two cereals would be suitable elements in one portfolio. From the diversification point of view, corn and oats also have their advantages, since very low coherence is found between these two agricultural commodities in all the wavelet scales.

REFERENCES


Received May 15, 2018
Accepted June 20, 2018
Published online January 12, 2018